



## Highlights

- A new approach is proposed for Temporal Reasoning in ASP;
- The approach takes advantage of the automata representation of  $LTL_f$  formulae;
- It is shown how to apply it for solving three DPM problems: Log Generation, Conformance Checking, and Query Checking;
- Poster based on work that appeared in [1, 2, 3]

## Declarative Process Mining

Declarative Process Mining [4] is a subfield of Process Mining where processes are modeled using constraint-based languages, such as DECLARE [5] or  $LTL_f$  [6].

## $LTL_f$

- Linear-Time Temporal logic on finite traces ( $LTL_f$ ) is a logic that allows expressing properties of finite sequences, called traces.
- Given a set  $\mathcal{P}$  of propositional symbols, the syntax is defined by the following grammar:

$$\varphi ::= A \mid \neg\varphi \mid \varphi_1 \wedge \varphi_2 \mid \mathbf{X}\varphi \mid \varphi_1 \mathbf{U}\varphi_2$$

with  $A \in \mathcal{P}$ .

- Given a formula  $\varphi$ , a trace  $\pi = \pi_1, \pi_2, \dots, \pi_{len(\pi)} \in (2^{\mathcal{P}})^+$ , and a time instant  $i$ , with  $1 \leq i \leq len(\pi)$ , the semantics is defined as follows:
  - $\pi, i \models A$  iff  $A \in \pi_i$ ,
  - $\pi, i \models \neg\varphi$  iff  $\pi, i \not\models \varphi$ ,
  - $\pi, i \models \varphi_1 \wedge \varphi_2$  iff  $\pi, i \models \varphi_1$  and  $\pi, i \models \varphi_2$ ,
  - $\pi, i \models \mathbf{X}\varphi$  if  $i < len(\pi)$  and  $\pi, i+1 \models \varphi$ ,
  - $\pi, i \models \varphi_1 \mathbf{U}\varphi_2$  iff  $\pi, j \models \varphi_2$  for some  $j$ , with  $i \leq j \leq len(\pi)$ , and  $\pi, k \models \varphi_1$  for all  $k = i, \dots, j-1$ .
- Common abbreviations used are:
  - $true, \rightarrow, \vee$
  - $\mathbf{F}\varphi \equiv true \mathbf{U}\varphi$
  - $\mathbf{G}\varphi \equiv \neg \mathbf{F}\neg\varphi$
  - $\varphi_1 \mathbf{W}\varphi_2 \equiv \varphi_1 \mathbf{U}\varphi_2 \vee \mathbf{G}\varphi_1$

## DECLARE as $LTL_f$

Template	Formula
<i>Absence</i> ( $a$ )	$\neg \mathbf{F}a$
<i>Existence</i> ( $a$ )	$\mathbf{F}a$
<i>Response</i> ( $a, b$ )	$\mathbf{G}(a \rightarrow \mathbf{F}b)$
<i>NotResponse</i> ( $a, b$ )	$\mathbf{G}(a \rightarrow \neg \mathbf{F}b)$
<i>RespondedExistence</i> ( $a, b$ )	$\mathbf{F}a \rightarrow \mathbf{F}b$
<i>AlternateResponse</i> ( $a, b$ )	$\mathbf{G}(a \rightarrow \mathbf{X}(\neg a \mathbf{U}b))$
<i>Precedence</i> ( $a, b$ )	$\neg b \mathbf{W}a$

## $LTL_f$ 2DFA

For each  $LTL_f$  formula, there exists a finite-state automaton that accepts exactly the traces satisfying the formula.

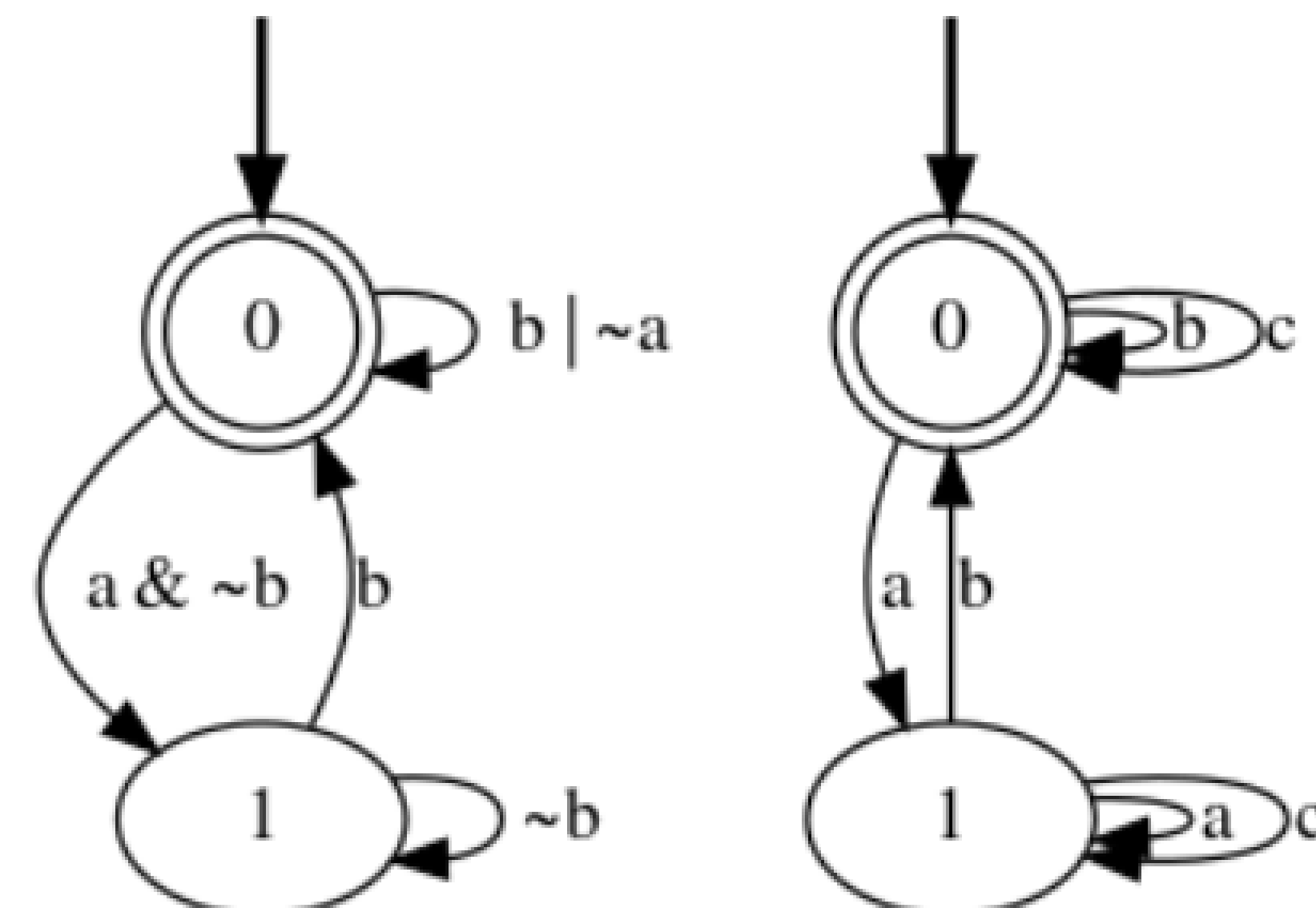


Figure: Automaton of *Response*( $a, b$ ) template: (left) as obtained by available  $LTL_f$  tools for conversion (right) simplified by exploiting that we work with process traces

## ASP

- Answer Set Programming [7] is a declarative problem solving approach inspired by Logic Programming and SAT.
- Given a problem, this is modeled as a logic program and is fed into an ASP system, such as *clingo* [8]. The system then computes the stable models of the program, each corresponding to a different solution to the problem.

## Encoding Temporal Problems in ASP

Given a problem involving temporal specifications one can represent the corresponding automata in ASP and simulate their running over a trace. The problems then reduce to checking whether the automata accept the trace.

```

automaton(s0, a, s1).
automaton(s1, b, s0).
automaton(s0, b, s0).
automaton(s0, c, s0).
automaton(s1, a, s1).
automaton(s1, c, s1).
initial(s0).
accepting(s0).

```

ASP encoding of *Response*( $a, b$ ).

## Problems

- Log generation: use generation rules for guessing a trace and a test rule for checking whether the trace is accepted.
- Conformance Checking: just check whether the traces are accepted.
- Query Checking: guess a template instantiation and check if the automata obtained accepts the log.

## Conclusions and Future Work

- We have seen how to solve DPM problems using ASP;
- The solution is based on exploiting the automata representation of the process models;
- The approach is applicable to many other DPM problems, e.g., Process Discovery and Trace Alignment;
- One could also consider more in general PM problems by using ASP for modeling Petri nets.

## References

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